

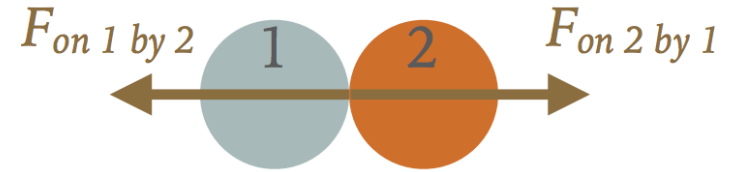
# CONSERVATION OF MOMENTUM

- Picture 2 billiard balls set on a head-on collision (ignore any retarding forces)
- After collision, the two momentum of the balls will change
- But the **sum** of the momenta will be the same before and after the collision

*Before:*



*During:*



*After:*



# CONSERVATION OF MOMENTUM

$$P_{\text{before}} = P_{\text{after}}$$

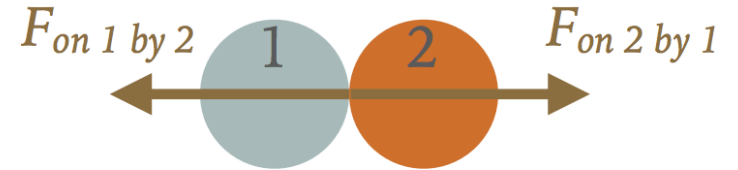
$$m_1 v_1 + m_2 v_2 = m_1 v_1' + m_2 v_2'$$

The total momentum of the  
two-ball system is **conserved**

*Before:*



*During:*



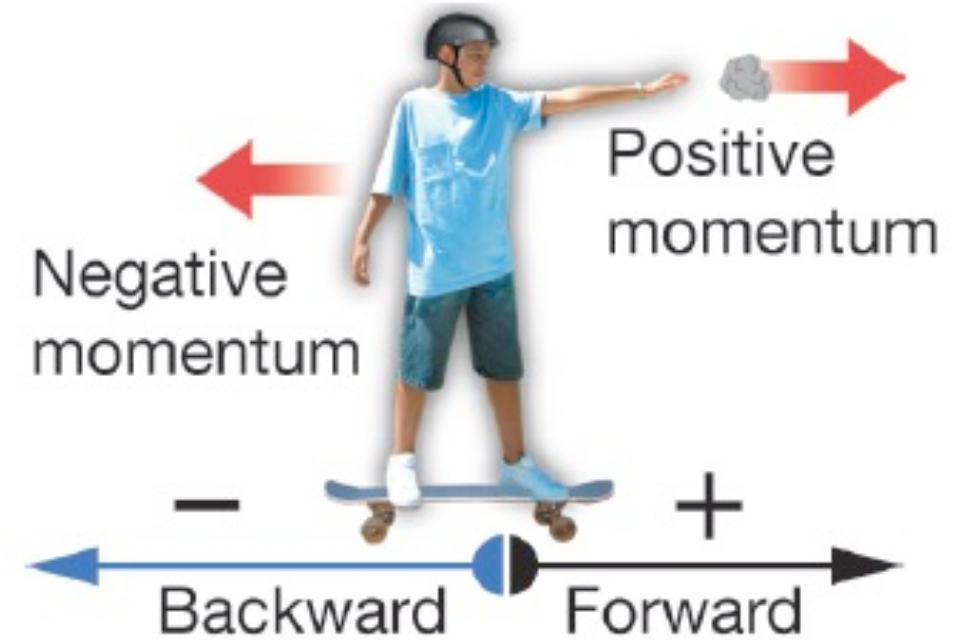
*After:*



## LAW OF CONSERVATION OF MOMENTUM

*The total momentum of an isolated system remains constant*

- **System:** Set of objects that interact with each other
- **Isolated system:** system in which the only forces present are those between the objects of the system



If you throw a rock forward from a skateboard, you will move backward in response.

KIRBY TURNS INTO A ROCK AND FREE FALLS. IS  
MOMENTUM CONSERVED?

It is if you include the  
Earth in your system!



# CONSERVATION OF MOMENTUM AND ROCKETS

- Before the engines fire, the total momentum (rocket + fuel) is zero
- Backward momentum of expelled exhaust = forward momentum of rocket
- Similar to Newton's 3<sup>rd</sup> Law!



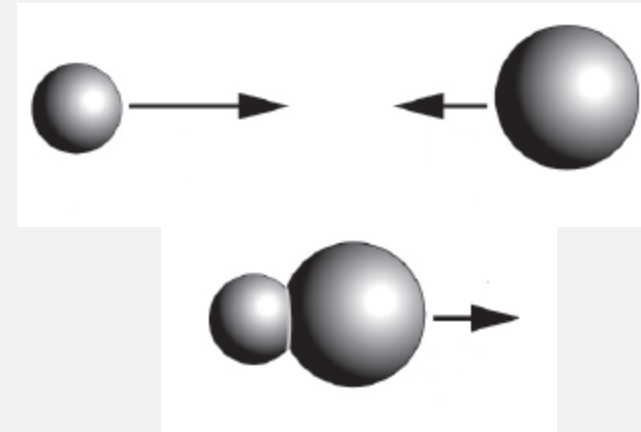
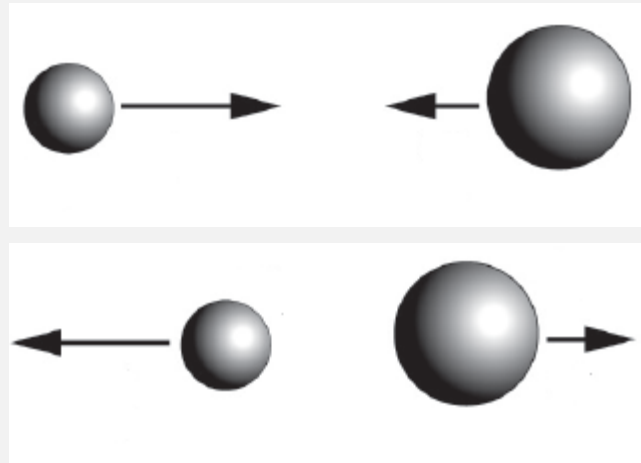
## RECOIL

- Calculate the recoil velocity of a 5.0 kg rifle that shoots a 0.050 kg bullet at 120 m/s
- $m_B v_B + m_R v_R = m_B v_B' + m_R v_R'$  ( $0 = 0.050\text{kg} \times 120\text{m/s} + 5.0\text{kg} + v_R'$ )
- $v_R' = -1.2 \text{ m/s}$
- What does the negative sign mean?



# COLLISIONS IN ONE DIMENSION

- A *collision* occurs when two or more objects hit each other.
- During a collision, momentum is transferred from one object to another, but **total momentum is conserved**
- Collisions can be *elastic* or *inelastic*.



# ELASTIC COLLISIONS

If the two objects is a collision are

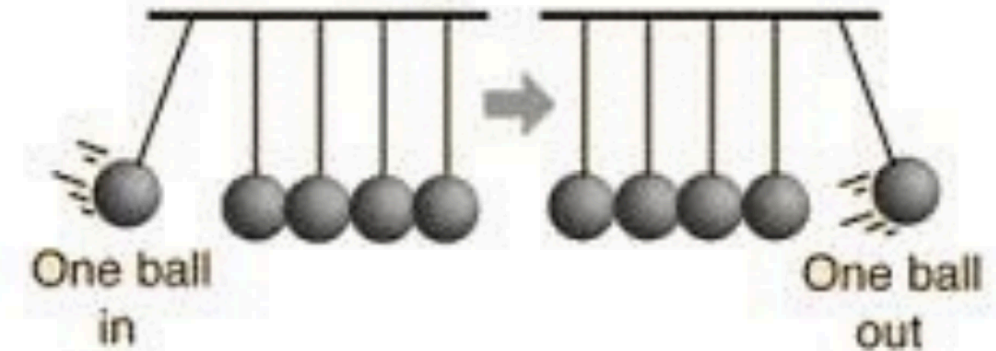
- Very hard
- No heat is produced in the collision

Then kinetic energy is also conserved

These collisions are **perfectly elastic**

Momentum in:  $mv =$  momentum out

Kinetic energy in:  $\frac{1}{2}mv^2 =$  kinetic energy out





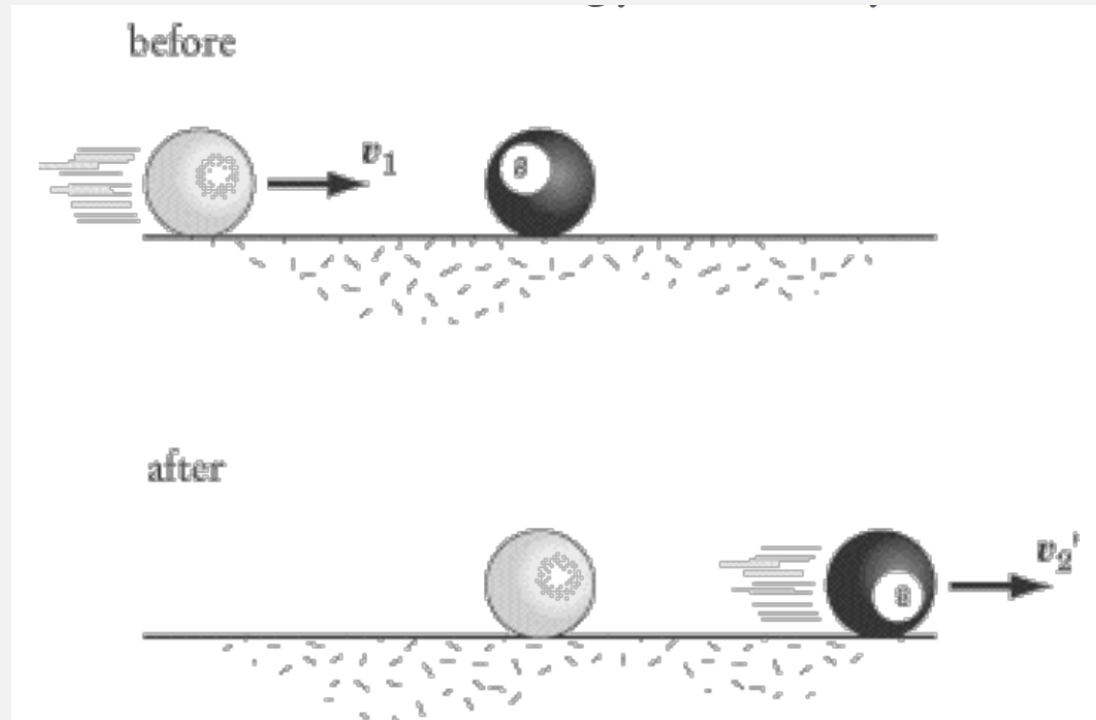
# ELASTIC COLLISIONS

A billiard ball of mass  $m$  moving with speed  $v$  collides head-on with another ball of equal mass at rest. What are the speeds of the two balls after the collision, assuming it is perfectly elastic and there is no spin?

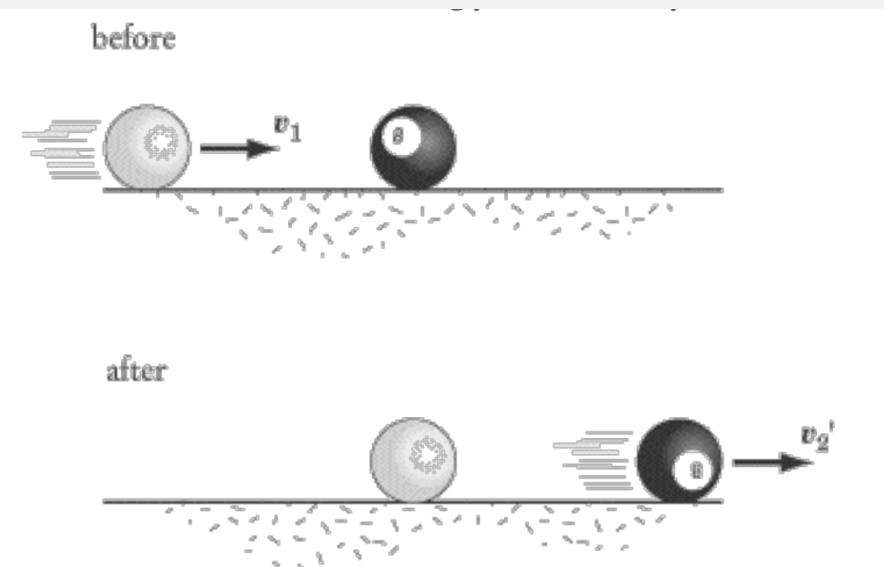
$$p_{\text{before}} = p_{\text{after}}$$

$$m_1 v_1 + m_2 v_2 = m_1 v_1' + m_2 v_2'$$

$$v_1' = 0, v_2' = v$$



# AN IMPORTANT DERIVATION: CONSERVATION OF KE AND CONSERVATION OF MOMENTUM



(Giancoli pg. 188-189)

# ELASTIC COLLISIONS

A proton of mass  $m_p = 1.67 \times 10^{-27}$  kg traveling at  $3.60 \times 10^4$  m/s has an elastic head-on collision with an alpha particle (helium nucleus,  $m_a = 6.64 \times 10^{-27}$  kg) initially at rest.

What are the velocities of the proton and helium nucleus after the collision?

$$\begin{aligned} p_{\text{before}} &= p_{\text{after}} & KE_i &= KE_f \\ m_1 v_1 + m_2 v_2 &= m_1 v_1' + m_2 v_2' \\ \mathbf{v}_1 - \mathbf{v}_2 &= \mathbf{v}_2' - \mathbf{v}_1' \end{aligned}$$

